

## Factoring Polynomials

1. First, look to see if there is something that all terms share that can be factored out (GCF).
2. Then, choose your method based on if you have a binomial, trinomial, or quadrinomial.

### Binomials

#### Difference of Squares

$$(a^2 - b^2) = (a + b)(a - b)$$

$$\text{ex: } (x^2 - 9) = (x + 3)(x - 3)$$

#### Difference of Cubes

$$(a^3 - b^3) = (a - b)(a^2 + ab + b^2)$$

$$\text{ex: } (x^3 - 8) = (x - 2)(x^2 + 2x + 4)$$

#### Sum of Cubes

$$(a^3 + b^3) = (a + b)(a^2 - ab + b^2)$$

$$\text{ex: } (x^3 + 8) = (x + 2)(x^2 - 2x + 4)$$



The signs follow S.O.A.P.

(Same, Opposite, Always Positive)

### Trinomials

#### Diamond Method

$$x^2 + 7x + 10$$

$$\begin{array}{ccc} & 10 & \\ 2 & \times & 5 \\ & 7 & \end{array}$$

See what **multiplies** to the top and **adds** to the bottom.

$$(x + 2)(x + 5)$$

#### Splitting the Middle Term (When you have a number in front of $x^2$ .)

$$2x^2 + 9x + 10$$

$$\begin{array}{ccc} & 20 & \\ 4 & \times & 5 \\ & 9 & \end{array}$$

← Multiply the first term and the last term to get the top number.

$$2x^2 + 4x + 5x + 10$$

$$(2x^2 + 4x) + (5x + 10)$$

$$2x(x + 2) + 5(x + 2)$$

$$(2x + 5)(x + 2)$$

Split the middle term into  $4x + 5x$ .

Use Factoring by Grouping (see below).

### Quadrinomials

#### Factoring by Grouping

$$2x^3 + 5x^2 + 4x + 10$$

$$(2x^3 + 5x^2) + (4x + 10)$$

$$x^2(2x + 5) + 2(2x + 5)$$

$$(x^2 + 2)(2x + 5)$$

Group first two terms and last two terms.

Factor.

Rearrange (by factoring again).